# Cyber-physical systems and their verification(2.8.2) TD nº 2 : Timed regular languages

### Reminder : two Alur's theorems

- 1. Given a timed automaton A one can compute a finite automaton B such that L(B) = Untime(L(A))
- 2. Universality problem "Does a timed automaton A accept all the timed words?" is undecidable

#### **Exercice 1** – Four languages

Are the following timed languages over  $\{a, b\}$  timed regular? Build a timed automaton or prove that it is impossible.

- **1.**  $L_1$ : timed words with the number of a being a prime integer.
- **2.** L<sub>2</sub> : timed words with the duration being a prime integer.
- **3.**  $L_3 = \{tatb\}$ . (with t staying for delay between events).
- **4.**  $L_4 = \{talasb|t + s = 2\}$ . Also, is it recognizable with a one-clock automaton?

## Exercice 2 – Folk's theorems — S. Tripakis

Prove that no algorithm given a timed automaton A

- answers YES or NO whether  $\overline{L(A)}$  is timed regular;
- and if the answer is YES builds a timed automaton B such that  $\overline{L(A)} = L(B)$ .

Hint : suppose that such an algorithm exists and use it to decide Universality.

**Remark :** (O. Finkel) deciding whether  $\overline{L(A)}$  is timed regular is also impossible.

#### Exercice 3 – Modeling and verification — easy exercise

**Romeo** wakes up between 6 and 7 o'clock, learns Timed automata for 6 to 8 hours, then swims for 2 to 3 hours, makes jogging for 2 to 4 hours (altogether he makes sport for less than 6 hours), and goes to "Chez Uppaal" bar for the rest of the day. He goes to bed at 22 hours.

**Juliet** is awake from 7 to 21, and during all that time she alternates 3 hours of learning Hybrid systems and 1 hour of hanging at "Chez Uppaal".

The **specification** says that they should never meet "Chez Uppaal".

- 1. Model Romeo and Juliet behaviors by timed automata.
- **2.** Represent the verification of the specification as emptiness checking for an intersection of timed regular languages. **Hint :** you will need a special event for their rendezvous.